

# Silicon Detector Results from the First Five-Tower Run of CDMS II

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We report results of a search for Weakly Interacting Massive Particles (WIMPs) with the Si detectors of the CDMS II experiment. This report describes a blind analysis of the first data taken with CDMS II's full complement of detectors in 2006-2007. Results from this exposure using the Ge detectors have already been presented. We observed no candidate WIMP-scattering events in an exposure of 55.9 kg-days before analysis cuts. These data set an upper limit of  $1.7 \times 10^{-41} \text{ cm}^2$  on the WIMP-nucleon spin-independent cross section of a 10 GeV/c<sup>2</sup> WIMP; this limit improves to  $8.3 \times 10^{-42} \text{ cm}^2$  in combination with previous Si data from this installation. These data exclude parameter space for spin-independent WIMP-nucleon elastic scattering that is relevant to recent searches for low-mass WIMPs.

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There is now overwhelming evidence that the bulk of the matter in our universe is in some nonluminous, non-baryonic form [1]. Though there is broad consensus on the amount of this dark matter present in the cosmos, its composition has thus far eluded laboratory investigations. Weakly Interacting Massive Particles (WIMPs) [2] – particles with masses between tens of GeV/c<sup>2</sup> and a few TeV/c<sup>2</sup> and interaction strengths characteristic of the weak force – form a leading class of candidates for this

dark matter. Particles of this type would be produced thermally in the early universe in roughly the correct amount, and are predicted by many theoretical extensions to the Standard Model of particle physics [1, 3]. If WIMPs do constitute the dark matter in our galaxy, they may be detectable through their elastic scattering off of nuclei in terrestrial particle detectors [4]. Numerous experimental groups have sought to detect such scattering events using a wide variety of technologies [5].

The Cryogenic Dark Matter Search (CDMS) collaboration seeks to identify nuclear recoils from WIMP interactions using semiconductor detectors operated at very low temperatures ( $\sim 40$  mK). These detectors use a simultaneous measurement of ionization and out-of-equilibrium phonons to identify such events among a far more numerous background of electron recoils. From 2003-2008 the collaboration operated CDMS II, an array of Ge and Si detectors located at the Soudan Underground Laboratory. Previous results from the CDMS II installation [6–9] have set stringent upper limits on the WIMP-nucleon scattering cross section and constrained some non-WIMP dark matter candidates [10].

This work presents results from a search for WIMP interactions in the CDMS II Si detectors during the first run of the experiment with its full complement of detectors. The lower atomic mass of Si generally makes it a less sensitive target for spin-independent (scalar) WIMP interactions, due to the coherent enhancement of the scattering cross section for heavy nuclei. The lower atomic mass of Si is advantageous in searches for WIMPs of relatively low mass, however, due to more favorable scattering kinematics. A WIMP of mass  $\lesssim 40$  GeV/ $c^2$  will impart more recoil energy to a Si atom than a Ge atom on average, so a WIMP of sufficiently low mass ( $M \lesssim 10$  GeV/ $c^2$  for CDMS II) will generate more detectable recoils in a Si detector at fixed energy threshold. New particles at such masses are generally disfavored in fits of supersymmetry models to precision electroweak data (*e.g.* [11]), but viable models in this regime do exist (*e.g.* [12]). Renewed interest in this mass range has been motivated by recent results from the DAMA/LIBRA [13], CoGeNT [14], and CRESST [15] experiments, which have been interpreted as possible evidence of WIMP scattering. CDMS has previously explored similar parameter space using dedicated low-threshold analyses of data from its shallow and deep runs [16].

In its final configuration, the CDMS II array consisted of 30 Z-sensitive ionization and phonon (ZIP) detectors: 19 Ge ( $\sim 239$  g each) and 11 Si ( $\sim 106$  g each), for a total of  $\sim 4.6$  kg of Ge and  $\sim 1.2$  kg of Si. Each CDMS detector is a semiconductor disk, 7.6 cm in diameter and 1 cm thick, instrumented to detect the phonons and ionization generated by particle impacts within the crystal. One flat face of each detector is instrumented with four readout channels composed of superconducting transition-edge sensors (TESs) to detect out-of-equilibrium phonons. The opposite flat face is divided into two concentric ionization electrodes: an inner (primary) electrode covering  $\sim 85\%$  of the detector surface and an outer guard ring. The latter defines a fiducial volume within each ZIP by identifying interactions near the detector rim, which may suffer from reduced ionization collection. We discriminate nuclear recoils from background electron recoils using the ratio of ionization to phonon recoil energy (“ionization yield”), with a misidentification rate for electron recoils of less than 1 in  $10^4$ . Electron recoils that occur within  $\sim 10$   $\mu\text{m}$  of a detector surface can be misclassified as nu-

clear recoils due to reduced ionization collection. Such surface events are identified by the faster arrival of their phonon signals, giving an overall misidentification rate for electron recoils of less than 1 in  $10^6$ .

This detector array was housed within a low-radioactivity cryogenic installation [8, 17] at the Soudan Underground Laboratory, Minnesota, U.S.A. The rock overburden above the Soudan facility (2090 meters water equivalent) reduces the flux of cosmogenic muons incident upon the detector installation by a factor of  $\sim 10^5$ , thus greatly reducing the background neutron flux. An outer hermetic layer of plastic scintillator identifies remaining cosmogenic muons entering the passive Pb and polyethylene shielding surrounding the detector volume.

We consider data taken with the Si detectors during the first two run periods of the full CDMS II detector installation, acquired between October 2006 and July 2007. The Ge results from this data set were described in a previous publication [8], which was released before the Si analysis was complete. Of the 11 Si detectors, five were excluded from the WIMP-search analysis: two due to wiring failures that led to incomplete collection of the ionization signal, one due to unstable response on one of its four phonon channels, and two due to inadequate rejection of surface events in the analysis chosen for this exposure. Periods of poor performance, as identified by a series of Kolmogorov-Smirnov tests, were also excluded from analysis. After all such exclusions, these data represent 55.9 kg-days of exposure with the remaining six Si detectors before selection of WIMP candidates.

The response of these detectors to electron recoils was calibrated using events from extensive exposures to radioactive  $^{133}\text{Ba}$  sources *in situ* at Soudan. Electron recoils from these sources were used to empirically characterize and correct for the dependence of phonon pulse shape on event position and energy. As in the analysis of the Ge detectors, events at large detector radii were excluded due to degraded performance of this correction technique. Because the Si detectors generally do not show a clear 356-keV spectral line from the  $^{133}\text{Ba}$  source, their ionization and phonon energy scales were calibrated using 356-keV events that share their energy with a neighboring detector.

The detectors’ response to nuclear recoils was characterized using neutron-scattering events from *in situ* calibration with a  $^{252}\text{Cf}$  source. The resulting nuclear recoil population was used to tune the various WIMP-selection criteria of this analysis, notably those for ionization yield and phonon timing. We have verified the calibration of the nuclear recoil energy scale by comparisons to Monte Carlo simulations of the  $^{252}\text{Cf}$  exposures, an analysis which will be described in a separate publication [18]. Such comparisons are particularly robust for the Si detectors, due to a fortuitous resonant feature in the Si-neutron elastic scattering cross section. This study indicates that our reconstructed energy may be 10% lower than the true recoil energy in the relevant energy range. This would slightly weaken our quoted

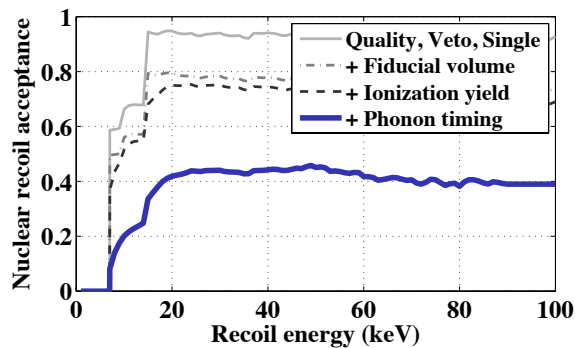


FIG. 1. Nuclear recoil acceptance as a function of recoil energy after successive application of each WIMP-selection criterion shown. The bold solid curve shows the overall efficiency of this analysis. The abrupt drops in acceptance at low recoil energies reflect the elevated energy thresholds chosen for some detectors.

results, as described below.

Candidate WIMP-scattering events were identified by a series of selection criteria. These criteria were defined in parallel with those described in [8] for the Ge detectors using the same techniques. As with the Ge detectors, all WIMP-selection criteria were defined blindly using calibration and masked WIMP-search data; for the latter, events in and near the WIMP-candidate region were automatically masked from the data set during analysis and thus had no impact on the definition of the selection criteria. A WIMP candidate was required to have phonon and ionization signals inconsistent with noise alone, to exhibit no coincident energy in the scintillating veto shield or in any of the other 29 ZIP detectors, and not to be coincident with beam spills of the NuMI neutrino beam [19]. We further demanded that any candidate event occur within the detector's fiducial volume and have ionization yield and phonon pulse timing consistent with a nuclear recoil. The recoil energy of each candidate event must also lie below 100 keV and above a detector-dependent threshold ranging from 7 to 15 keV, also chosen blindly based upon calibration data. Fig. 1 shows the estimated fraction of WIMP-scatter events that would be accepted by these signal criteria. Signal acceptance was measured using nuclear recoils from  $^{252}\text{Cf}$  calibration. Monte Carlo simulations indicate that multiple-scattered neutrons in calibration data reduce the measured efficiency of the fiducial volume selection by  $\sim 5.5\%$  with respect to the true value for single-scatter nuclear recoils, so we have scaled its efficiency upward by this amount. Signal acceptance is  $\sim 40\%$  at most recoil energies, somewhat higher than that of the Ge analysis. After applying all selection criteria, the exposure of this analysis is equivalent to 19.7 kg-days over a recoil energy range of 7-100 keV for a WIMP of mass 60 GeV/ $c^2$ .

Neutrons from cosmogenic or radioactive processes can produce nuclear recoils that are indistinguishable from those from an incident WIMP. Simulations of the rates

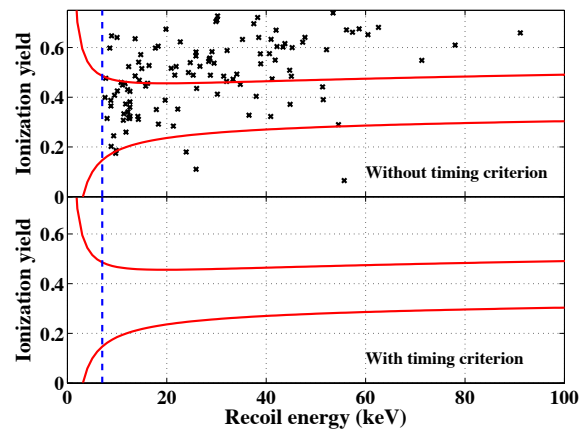


FIG. 2. Ionization yield versus recoil energy in all detectors included in this analysis for events passing all signal criteria except (*top*) and including (*bottom*) the phonon timing criterion. The curved lines indicate the signal region ( $\pm 2\sigma$  from mean nuclear recoil yield) between 7 and 100 keV recoil energies. Electron recoils in the detector bulk have yield near unity, above the vertical scale limits.

of these processes using GEANT4 and FLUKA lead us to expect  $< 0.1$  false candidate events in the Si detectors from neutrons in this exposure.

A greater source of background is the misidentification of surface electron recoils, which may suffer from reduced ionization yield. As in the Ge analysis, we developed a Bayesian estimate of the rate of misidentified surface events based upon the observed performance of the phonon timing cut for events near the WIMP-search signal region [20]. For the Si analysis we based our model only upon multiple-scatter events within the ionization yield acceptance region, since other event samples incorporated into the Ge analysis were found to be less reliable predictors for Si. This model is not applicable to detectors at the top and bottom of their respective stacks, since it is impossible to identify multiple-scatter events on the outside face of such detectors. We thus decided to exclude detectors in these positions from this blind analysis. The final model predicts an average of  $1.1^{+0.9}_{-0.6}(\text{stat.}) \pm 0.1(\text{syst.})$  misidentified surface events in the six Si detectors during this exposure.

After all WIMP-selection criteria were defined and the background estimate finalized, the signal regions of the Si detectors were unmasked on December 3, 2008. No candidate WIMP-scattering events were observed. Fig. 2 illustrates the distribution of events in and near the signal region of the WIMP-search data set before (*top*) and after (*bottom*) application of the phonon timing criterion. Fig. 3 shows an alternate view of these events, expressed in “normalized” versions of yield and timing that are transformed so that the WIMP acceptance regions of all detectors coincide.

This null result constrains the available parameter space of WIMP dark matter models. We compute upper limits on the WIMP-nucleon scattering cross section

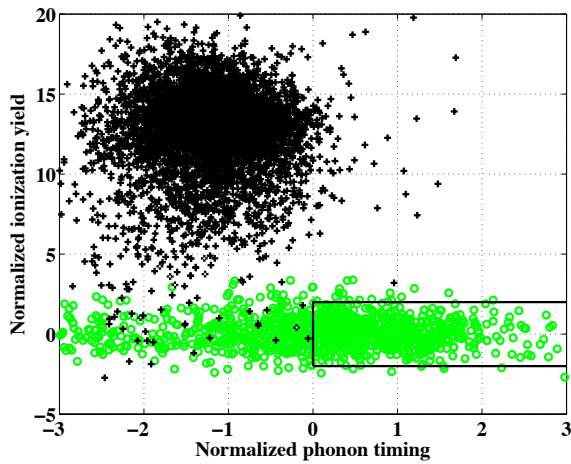


FIG. 3. Normalized ionization yield (standard deviations from the nuclear recoil band centroid) versus normalized phonon timing parameter ( $\mu\text{s}$  from the timing criterion) for events in all detectors from the WIMP-search data set passing all other selection criteria. The black box indicates the WIMP candidate selection region. Also plotted are nuclear recoils from  $^{252}\text{Cf}$  calibration data (*light, green dots*).

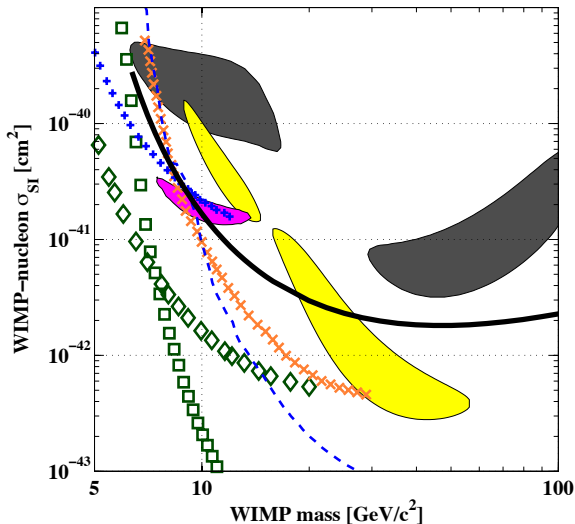


FIG. 4. Comparison of 90% C.L. upper limits from these data (*solid*) with those from CDMS II Ge [9, 16] (*dash, +*), EDELWEISS [21] (*x*), XENON10 [22] (S2-only analysis,  $\diamond$ ), and XENON100 [23] ( $\square$ ). The filled regions identify regions of interest associated with data from DAMA/LIBRA [13, 24] (*dark grey*, 99.7% C.L.), CoGeNT [25] as interpreted by Kelso *et al.* [26] (*magenta*, 90% C.L., including the effect of a residual surface event contamination), and CRESST II [15] (*yellow*, 95.4% C.L.).

using Yellin’s optimum interval method [27]; this is equivalent to a Poisson upper limit in the present zero-event

case, but generally results in a stronger limit when events are observed. We work within the “standard” halo model described in [28], assuming a galactic escape velocity of 544 km/s [29]. Fig. 4 shows upper limits on the WIMP-nucleon spin-independent scattering cross section at the 90% confidence level from CDMS II data and a selection of other recent results. The present data set an upper limit of  $1.66 \times 10^{-41}$  ( $1.86 \times 10^{-42}$ )  $\text{cm}^2$  for a WIMP of mass 10 (60)  $\text{GeV}/c^2$ . The effect of a  $\sim 10\%$  increase in our nuclear recoil energy scale is well approximated below 20  $\text{GeV}/c^2$  by shifting the limit curve parallel to the mass axis by  $\sim 7\%$ . Since unblinding these data, recent results from CDMS II [9, 16], EDELWEISS [21], XENON100 [23], and a novel low-threshold analysis of data from XENON10 [22] also disfavor this parameter space.

Fig. 4 also compares these results to three recent results that have been interpreted as evidence for WIMP interactions. The CoGeNT experiment has observed an excess of events in their Ge crystal above expected background [14] and an annual modulation of their low-energy event rate [25, 26], similar to what might be expected from interactions of a low-mass WIMP. The CRESST II experiment has also observed an excess of events above their background model [15]. This null result disfavors portions of the best-fit regions suggested by the authors in both cases, as well as an interpretation of the DAMA/LIBRA annual modulation signal in terms of spin-independent scattering [24].

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